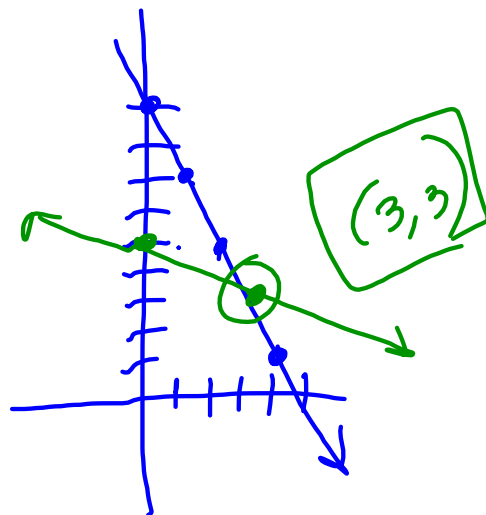


22.

$$\begin{array}{r} 2x + y = 9 \\ -2x \quad \quad -2x \\ \hline y = -2x + 9 \\ m = -2 \\ b = 9 \end{array}$$

$$\begin{array}{r} 2x + 3y = 15 \\ -2x \quad \quad -2x \\ \hline 3y = -2x + 15 \\ \frac{3y}{3} = \frac{-2x}{3} + \frac{15}{3} \\ y = \frac{-2}{3}x + 5 \\ m = \frac{-2}{3} \\ b = 5 \end{array}$$



## Warm-up: Yikes!!

Suppose  $a = 2b + 3$ ,  $b = 4c + 5$ ,  
 $c = 6d + 7$ , and  $d = 8$ . What is  
the value of  $a$ ?

$$c = 6(8) + 7$$
$$48 + 7$$

$$c = 55$$

$$b = 4(55) + 5$$
$$220 + 5$$
$$b = 225$$

$$a = 2(225) + 3$$
$$450 + 3$$

$$a = 453$$

## 6.2 Solve Linear Systems by Substitution

*Before*

You solved systems of linear equations by graphing.

*Now*

You will solve systems of linear equations by substitution.

*Why?*

So you can find tubing costs, as in Ex. 32.



**GOAL:** Solve systems of linear equations exactly and approximately.

## Example 1!

Solve by using substitution:

$$\begin{array}{l}
 x = 3y + 5 \\
 2x - 4y = 12 \\
 \hline
 2(3y + 5) - 4y = 12 \\
 6y + 10 - 4y = 12 \\
 2y + 10 = 12 \\
 \quad -10 \quad -10 \\
 \hline
 2y = 2 \\
 \frac{2y}{2} = \frac{2}{2} \\
 y = 1 \\
 \hline
 x = 3y + 5 \\
 x = 3(1) + 5 \\
 x = 8
 \end{array}$$

$(x, y)$   
 $(8, 1)$

## Example 2!

Solve by using substitution:

$$\begin{array}{l} \boxed{y} = \boxed{x - 1} \\ 4\bar{x} - \boxed{y} = 19 \end{array}$$

$4x - (x - 1) = 19$

$$4x - x + 1 = 19$$
$$3x + 1 = 19$$
$$\begin{array}{r} -1 \quad -1 \\ \hline 3x = 18 \\ \frac{3x}{3} = \frac{18}{3} \\ x = 6 \end{array}$$

$y = x - 1$   
 $y = 6 - 1$   
 $y = 5$

$(6, 5)$

### Example 3-tougher!

Solve by using substitution:

$$\begin{array}{l}
 20x - 30y = -50 \\
 x + 2y = 1 \quad \rightarrow \quad \boxed{x = 1 - 2y} \\
 \begin{array}{r}
 \curvearrowright \\
 20(1 - 2y) - 30y = -50 \\
 20 - 40y - 30y = -50 \\
 \underline{-20} \quad \underline{-70y} = \underline{-50} \\
 \underline{-20} \quad \underline{-70y} = \underline{-50} \\
 \underline{-70y} = \underline{-70} \\
 \underline{-70} \quad \underline{-70} \\
 y = 1
 \end{array} \\
 \begin{array}{l}
 x = 1 - 2(1) \\
 x = 1 - 2 \\
 x = -1
 \end{array} \\
 \boxed{(-1, 1)}
 \end{array}$$

### Example 4-same idea!

Solve by using substitution:

$$5x + 4y = 32$$

$$9x - y = 33$$

Handwritten solution steps:

$$5x + 4y = 32$$

$$9x - y = 33$$

$$-9x \quad -9x$$


---


$$-y = 33 - 9x$$

$$\underline{-1} \quad \underline{-1} \quad \underline{-1}$$

$$-y = -33 + 9x$$

$$y = -33 + 9(4)$$

$$y = -33 + 36$$

$$y = 3$$

$$(4, 3)$$
  

$$5x + 4(-33 + 9x) = 32$$

$$5x - 132 + 36x = 32$$

$$41x - 132 = 32$$

$$\quad +132 \quad +132$$


---


$$41x = 164$$

$$\frac{41x}{41} = \frac{164}{41}$$

$$x = 4$$

## Last One: Word Problem!

The owners of a carnival have found that twice as many children as adults come to the carnival. Solve a system to estimate the number of children and the number of adults at the carnival when 3,570 people attend.

$$\boxed{C} = \boxed{2A}$$

$$C = 2(1190)$$

$$C = 2380$$

$$\boxed{C} + A = 3570$$

$$2A + A = 3570$$

$$\frac{3A = 3570}{3}$$

$$A = 1190$$



Homework 6.2:  
p.381: 4,5,6,10,16,28