

Math Studies study guide

 name _____
 period ____

 1) If $g(x) = 5^{-x}$, find:
a $g(1)$

a) $5^{-1} = \left(\frac{1}{5}\right)$

b $g(3)$

b) $5^{-3} = \frac{1}{5^3}$
 $\left(\frac{1}{125}\right)$

c $g(0)$

c) $5^0 = 1$

d $g(-2)$

d) $5^{-2} = 25$

e $g(-3)$

e) _____
 $5^3 = 125$

 2) Given $f(x) = 4\left(\frac{1}{2}\right)^x + 3$

 a) identify the y-intercept $(0, 7)$
 $\text{let } x=0$

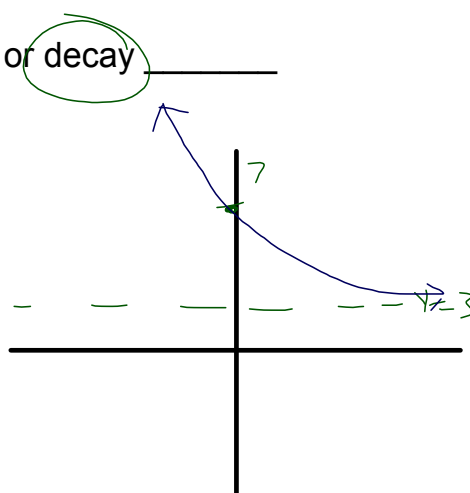
 b) identify the horizontal asymptote $y = 3$

c) identify the equation as exponential growth or decay _____

 d) as $x \Rightarrow \infty$, $y \Rightarrow 3$
 $x \rightarrow -\infty, y \rightarrow \infty$

e) sketch the curve on axis below

(label appropriate parts)



3) Solve each equation: (show how to solve for (t) by hand)

a) $4^t = 200$

$\ln 4^t = \ln 200$

$t \ln 4 = \ln 200$

$t = \frac{\ln 200}{\ln 4} = 3.82$

a) _____

b) $720\left(\frac{1}{3}\right)^x = 120$

$\log \frac{1}{3}^x = \log \frac{1}{6}$

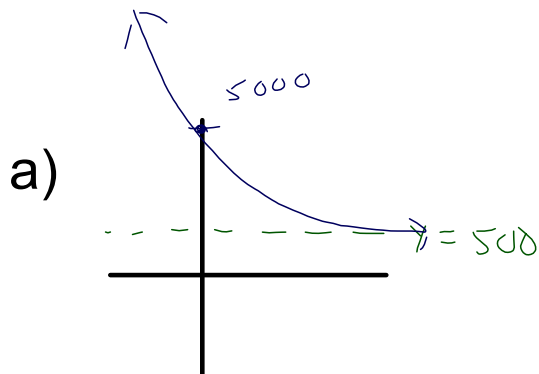
$x \log \frac{1}{3} = \log \frac{1}{6}$

$x = \frac{\log \frac{1}{6}}{\log \frac{1}{3}} = 1.63$

b) _____

4) The value of a car depreciates according to the formula $C(t) = 4500 \times (0.68)^t + 500$ euros, where t is the age of the car in years.

- a Sketch a graph of $C(t)$ against t .
 b What was the initial cost of the car?
 c How much is the car worth after $4\frac{1}{2}$ years?
 d State the equation of the horizontal asymptote of $C(t)$. What does this mean?
 e How long will it take for the car's value to drop to €1000?



b) $C(0) = 5000$

c) $C(4.5) = 1293.42$

d) $y = 500$

e) _____

$$1000 = 4500 \times (0.68)^t + 500$$

$$500 = 4500 \cdot (0.68)^t$$

$$\frac{1}{9} = (0.68)^t$$

$$\frac{\ln\left(\frac{1}{9}\right)}{\ln(0.68)} = t$$

$$t = 5.69727$$

5 years 8 months

